

Ans. to the Q. No 2

It is given in the question that the null space of A is a line, thus it can be interpreted that it is 1-dimensional subspace. Consider the rank nullity theorem:

$$P(A) + \text{nullity}(A) = \dim(A)$$

Note. $P(A)$ is the rank of A .

Putting the values in the above equation

$$P = (A) + 1 = 3$$

$$P = (A) = 2$$

Hence it can be said that it is the dimension of its row or column space. Thus it can be said that column space cannot be a line, but it will be a plane.

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Ans to the QNO-3

Relating the Determinant to the characteristic Polynomial. The key to this problem lies in understanding the relationship between the determinant of a matrix and its characteristic Polynomial.

We know that $P(\lambda) = \det(A - \lambda I)$. if we evaluate $P(0)$, we get: $P(0) = \det(A - 0I) = \det(A)$

*Evaluating the characteristic Polynomial. We are given $P(\lambda) = \lambda^3 - 2\lambda^2 + \lambda + 5$. To find the determinant of A we simply need to evaluate $P(0)$:

$$P(0) = (0)^3 - 2(0)^2 + (0) + 5 = 5.$$

Therefore the determinant to matrix A denoted as $\det(A)$, is $\dots 5$.

Ans. to the Q. No. 1

□ The Rank-nullity theorem :- The Rank-nullity theorem states that for any matrix A the rank of A (the dimension of the column space) equals the number of columns of A .

In summary.

matrix size	max Rank	min nullity
4×4	4	0
3×5	3	2
5×3	3	0