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Course - Differential Equation And Fourier Analysis.

Course code - MAT 325

Answer to the Question No-1

① (i)  $y = e^{3x+2}$

$$y_1 = \frac{dy}{dx} = e^{3x+2} \frac{d}{dx} (3x+2)$$

$$= e^{3x+2} (3 \cdot 1 + 0)$$

$$= 3e^{3x+2}$$

$$y_2 = \frac{y_1 y}{dx^2} = 3 \left[ \frac{d}{dx} (e^{3x+2}) \right]$$

$$= 3 (3e^{3x+2})$$

$$= 9e^{3x+2}$$

$$= 9y \text{ (Ans)}$$

②  ~~$y = \log x + ax$~~

(2)

Ans: (11)

$$y = \log x + ax$$

$$\frac{dy}{dx} = \frac{1}{x} + a$$

$$\therefore y_1 = \frac{1}{x} + a$$

$$\frac{y_2 y}{dx^2} = \frac{d}{dx} \left( \frac{1}{x} + a \right)$$

$$= -\frac{1}{x^2}$$

$$y_2 = -\frac{1}{x^2} \text{ Ans}$$

Answer to the question - 2

Ans:

$$f(x) = 3x^2 - 2x + 4$$

$$f'(x) = \frac{d}{dx}(3x^2) - \frac{d}{dx}(2x) + \frac{d}{dx} \cdot 4$$

$$= 6x - 2$$

at,  $x = 0$  slope

$$m = f'(0) = 3 \cdot 0^2 - 2$$

$$= -2$$

$$f(0) = 3 \cdot 0^2 - 2 \cdot 0 + 4$$

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So the point is (0, 4)

So the equation is.

$$y - y_0 = m(x - x_0)$$

$$\begin{cases} m = -2 \\ x_0 = 0 \\ y_0 = 4 \end{cases}$$

$$y - 4 = -2(x - 0)$$

$$\Rightarrow y = -2x - 4$$

Answer to the question - 4

Ans:

$$y = x^2 - 2x + 3$$

$$\Rightarrow \frac{dy}{dx} = 2x - 2$$

Now;  $2x - 2 = 0$

$$x = 1$$

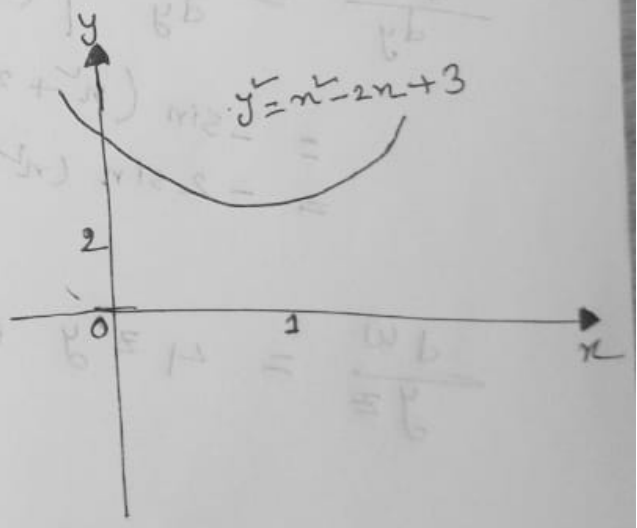
put  $x = 1$  at  $y$ .

$$y = 1^2 - 2 \cdot 1 + 3$$

$$= 1 - 2 + 3$$

$$= 2$$

$\therefore (x, y) = (1, 2)$  Ans



Answer to the Question NO-5 (4)

Ans:  $w = \cos(x^2 + 2y) - e^{4x - z^4 y} + y^3$

$$\frac{dw}{dx} = \frac{d}{dx} \left[ \cos(x^2 + 2y) - e^{4x - z^4 y} + y^3 \right]$$

$$= \sin(x^2 + 2y) \cdot (2x) - (e^{4x - z^4 y}) \cdot 4$$

$$= -2x \sin(x^2 + 2y) - 4e^{4x - z^4 y}$$

$$\frac{dw}{dy} = \frac{d}{dy} \left[ \cos(x^2 + 2y) - e^{4x - z^4 y} + y^3 \right]$$

$$= -\sin(x^2 + 2y) \cdot 2 + 3y^2$$

$$= -2\sin(x^2 + 2y) + 3y^2$$

$$\frac{dw}{dz} = 4z^3 y e^{(4x - z^4 y)}$$

————— x —————

Ans to the que no-3.

To find the second order differential equation for 'y' with respect to 'x', will first differentiate the given equation with respect to 'x' multiple time.

Given equation,

$$\frac{d^2y}{dx^2} + 3 \frac{d^2y}{dx} - 4y = x \cdot e^x$$

Let's differentiate it step by step.

① Take the first derivative of both sides with respect to

x :-

$$\frac{d}{dx} \left( \frac{d^2y}{dx^2} \right) + \frac{d}{dx} \left( 3 \frac{d^2y}{dx} \right) - \frac{d}{dx} (4y) = \frac{d}{dx} (x \cdot e^x)$$

$$\Rightarrow \frac{d}{dx} \left( \frac{d^2y}{dx^2} \right) + 3 \frac{d}{dx} \left( \frac{d^2y}{dx} \right) - 4 \frac{dy}{dx} = e^x + x e^x$$

$$\Rightarrow \frac{d^2}{dx^2} \left( \frac{d^2y}{dx^2} \right) + 3 \frac{d^2}{dx^2} \left( \frac{d^2y}{dx} \right) - 4 \frac{d^2y}{dx^2} = e^x + x e^x$$

$$\Rightarrow \frac{d^4y}{dx^4} + 3 \frac{d^3y}{dx^3} - 4 \frac{d^2y}{dx^2} = e^x + x e^x$$

So the

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So, the second-order differential equation for  $y$  with respect to  $x$  is:

$$\frac{d^2 y}{dx^2} + 3 \frac{d^3 y}{dx^3} - 4 \frac{dy}{dx} = e^x + x e^x.$$

Ans.